'boundaries' will cause addition of chains in a more irregular, less parallel fashion than in the early stages.

It has not been possible so far to examine the spectrum of 'basic' particles, nor does the work suggest the reason why the production of primary particles ceases. Nevertheless, this comparatively simple experiment in

Raman spectroscopy suggests an interesting picture for the build-up of PVC particles.

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# Prediction of swelling of polymers in 2 and 3 component solvent mixtures 

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Froehling et al. ${ }^{1}$ have shown how the vector concept of Hildebrand's solubility parameter may be used to predict the proportions in which two solvents should be mixed in order to obtain maximum swelling of a given polymer. In the present Note, the concept is formalized and extended to mixtures of three solvents. As methods of vector algebra will be employed to this end, they will first be applied to Froehling's problem, and a simple formula stated for the composition of the mixture of two solvents, or of a solvent and nonsolvent, which will give maximum swelling.

Hansen ${ }^{2}$ considered the solubility parameter to be the resultant of three components due to dispersion forces, to polar forces and to forces arising out of hydrogen bonding. The three components are not arithmetically additive, but lie as vectors along orthogonal axes. The end-point of the radius vector thus represents Hildebrand's solubility parameter in the three-component space. Using the value of the components given by Hansen ${ }^{2}$ and by Koenhen and Smolders ${ }^{3}$, and the equation:

$$
\left(\delta_{i}\right)_{m}=\phi_{1}\left(\delta_{i}\right)_{1}+\phi_{2}\left(\delta_{i}\right)_{2} \quad i=p, d, h(1)
$$

Froehling calculated the components of the solubility parameter of a mixture of two solvents.

In studying the swelling of polymers in such mixtures, Froehling compared
the proportion of solvent mixture imbibed by the polymer with the distance $\Delta$ between the points in space representing the solubility parameter of the polymer (such as $P$ in Figure 1), and the point representing the solubility parameter of the mixture such as $X$. Comparison of the two showed that, in general, the composition of a mixture which gives a maximum imbibition corresponds to a minimum $\Delta$. This situation exists when the mixture is defined by $M$ such that $P M$ and $A B$ are perpendicular.

The notation which we shall use in the following makes for simplicity and ease of writing. Instead of the subscripts $d, p$ and $h$, we shall use 1,2 and 3. The solubility parameters will be referred to by the lower case letter corresponding to the solvent component in the mixture, or the mixture itself, or the polymer. Thus $a_{1}$ is the dispersion component of the solubility parameter of solvent $A, m_{2}$ is the polar
component of the parameter of mixture $M$, and $p_{3}$ is the hydrogen bonding component of the parameter for polymer $P$. Values for these components may be found in refs 2 and 3.

For our present purposes, use is made of Froehlings Figure $I$ with the $\delta_{d}, \delta_{p}$ ( 1 and 2 in our notation) axes rotated by a right angle. Since $P M$ and $A B$ are orthogonal, the scalar or dot product of the vectors lying along the lines must vanish and therefore (see Figure 1):

$$
\begin{align*}
& \left(m_{1}-p_{1}\right)\left(b_{1}-a_{1}\right)+ \\
& \left(m_{2}-p_{2}\right)\left(b_{2}-a_{2}\right)+ \\
& \left(m_{3}-p_{3}\right)\left(b_{3}-a_{3}\right)=0 \tag{2}
\end{align*}
$$

For the line $A B$, we have:
$\frac{m_{1}-a_{1}}{b_{1}-l_{1}}=\frac{m_{2}-a_{2}}{b_{2}-a_{2}}=\frac{m_{3}-a_{3}}{b_{3}-a_{3}}$
We may combine (2) with (3) and simplify to obtain the expressions:
$m_{1}=a_{1}+\frac{\left(p_{1}-a_{1}\right)\left(b_{1}-a_{1}\right)+\left(p_{2}-a_{2}\right)\left(b_{2}-a_{2}\right)+\left(p_{3}-a_{3}\right)\left(b_{3}-a_{3}\right)}{\left(b_{1}-a_{1}\right)^{2}+\left(b_{2}-a_{2}\right)^{2}+\left(b_{3}-a_{3}\right)^{2}}\left(b_{1}-a_{1}\right)$
and substituting in (1), we have
$\Phi_{a}=1-\frac{\left(p_{1}-a_{1}\right)\left(b_{1}-a_{1}\right)+\left(p_{2}-a_{2}\right)\left(b_{2}-a_{2}\right)+\left(p_{3}-a_{3}\right)\left(b_{3}-a_{3}\right)}{\left(b_{1}-a_{1}\right)^{2}+\left(b_{2}-a_{2}\right)^{2}+\left(b_{3}-a_{3}\right)^{2}}=1-\Phi_{b}$


Figure 1 Spatial representation of 2 component solvent mixture - polymer interaction
where $\Phi_{a}$ is the volume fraction of solvent $A$ in the mixture $M$ of $A$ and $B$. Strict attention must be paid to the signs of these differences.

## Three component mixtures

Extending these considerations to mixtures of three non-interacting solvents or non-solvents, see Figure 2, we note that the vectors representing the lines joining $M$ to each of the vertices of the triangle $A, B$ and $C$ must be coplanar, while simultaneously $P M$ must be orthogonal to any two sides of the triangle. (The orthogonality to the third side is accounted for automatically. In other works $M A \cdot(\overline{M B} \times \overline{M C})$ $=0 . P M \cdot A B=0$ and $P M \cdot B C=0$. These may be manipulated into the following simple forms:

$$
\begin{align*}
& \left|\begin{array}{lll}
m_{1} & m_{1} & m_{1} \\
b_{1} & b_{1} & b_{1} \\
c_{1} & c_{2} & c_{3}
\end{array}\right|+\left|\begin{array}{lll}
a_{1} & a_{2} & a_{3} \\
m_{1} & m_{2} & m_{3} \\
c_{1} & c_{2} & c_{3}
\end{array}\right|+ \\
& \left|\begin{array}{lll}
a_{1} & a_{2} & a_{3} \\
b_{1} & b_{2} & b_{3} \\
m_{1} & m_{2} & m_{3}
\end{array}\right|=\left|\begin{array}{lll}
a_{1} & a_{2} & a_{3} \\
b_{1} & b_{2} & b_{3} \\
c_{1} & c_{2} & c_{3}
\end{array}\right|  \tag{5}\\
& m_{1}\left(a_{1}-b_{1}\right)+m_{2}\left(a_{2}-b_{2}\right)+ \\
& m_{3}\left(a_{3}-b_{3}\right)= \\
& p_{1}\left(a_{1}-b_{1}\right)+p_{2}\left(a_{2}-b_{2}\right)+p_{3}\left(a_{3}-b_{3}\right)
\end{align*}
$$

$$
m_{1}\left(a_{1}-c_{1}\right)+m_{2}\left(a_{2}-c_{2}\right)+
$$

$$
m_{3}\left(a_{3}-c_{3}\right)=
$$

$p_{1}\left(a_{1}-c_{1}\right)+p_{2}\left(a_{2}-c_{2}\right)+p_{3}\left(a_{3}-c_{3}\right)$

The length $\Delta$ of the line $P M$ is an inverse measure of the interaction between the solvent mixture and the polymer, and is easily calculated.

For calculations by hand or pocket calculator, equation (5) must be expanded. $m_{1}, m_{2}$ and $m_{3}$ for the 'best' mixed solvent having been determined, we may now proceed to determine $\phi_{a}$, $\phi_{b}$ and $\phi_{c}\left(=1-\phi_{a}-\phi_{b}\right)$ from*:
$\phi_{a} a_{1}+\left(\phi_{b}+\phi_{c}\right)\left(\phi_{b} b_{1}+\phi_{c} c_{1}\right)=m_{1}$
$\phi_{a} a_{2}+\left(\phi_{b}+\phi_{c}\right)\left(\phi_{b} b_{2}+\phi_{c} c_{2}\right)=m_{2}$
$\phi_{a} a_{3}+\left(\phi_{b}+\phi_{c}\right)\left(\phi_{b} b_{3}+\phi_{c} c_{3}\right)=m_{3}$

## RESULTS AND DISCUSSIONS

Table 1 presents data and calculated results for mixtures of optimum solubility (or swelling) towards specified polymers. For the purpose of this paper, optimum solubility implies merely the shortest distance between $P$ and the plane of $A B C$; it does not mean that there is real solubility for the given mixture, or that solubility is not equally observed with other proportions of the individual solvents. Furthermore, no suggestion is made that solutions of the polymers in the solvent mixture will have a low viscosity; on the contrary, there is good reason to believe that the viscosity of such solutions is very nearly the maximum attainable.

Particular attention must be paid to two points in interpreting the results. In the first place, there is considerable uncertainty in the values of solubility parameter components. Where the polar and dispersion components of two solvents are very close toge ther, a small uncertainty in the value of the third component may cause very big differences in the values of $m_{1}, m_{2}, m_{3}$ and $\Delta$ calculated. Secondly, the individual

[^0]The author will be pleased to save readers with access to APL both time and trouble by supplying this program on application.
solvents may interact, in which case the interpretation given does not hold.
Froehling presents such an anomaly when he considers the mixture butyl acetate and nitromethane acting on PVC.

Inspecting case 1 in Table 1, we note that the optimum solvent ratios for toluene/hexane/chlorobenzene contains toluene in a negative quantity. From a geometrical point of view, this merely implies that $M$ in on the opposite side of the line connecting the points for hexane and chlorobenzene as compared with the point for toluene. However, this can be given an interesting physical explanation when comparison is made with cases 4,5 and 6 . It appears that chlorobenzene is a considerably poorer solvent for polybutadiene than either toluene or hexane, and its addition reduces the solubility of a mixture of toluene and hexane towards polybutadiene (case 2).

Proceeding to PAN, and considering $\Delta$ as an (inverse) indicator of solubility, it will be seen that of the cases studied, mix 10 has the smallest value of $\Delta$ amongst the 3 component mixes. It would seem that a volume fraction of 0.015 n-propanol would not be very important, but if mix 10 is compared with mix 8 (the mixes being not very different in their main components) it will be seen that this very small quantity of alcohol increases solubility considerably. On the other hand, a small quantity ( $1.3 \mathrm{vol} \%$ ) of n -butyl acetate increases the solubility only slightly (mix No 11).

Of the other combinations calculated, combination 17 must be taken with very great caution. Hansen ${ }^{2}$ makes no claim for any accuracy whatsoever, and there is much doubt if the propanol/ water mixture and trichlorethylene are mutually soluble.

PET appears to be soluble in several solvent combinations with little advantage of one over another.


Figure 2 Spatial representation of 3 component solvent mixture - polymer interaction

Table 1 Calculated polymer/solvent mixture interactions: solvent fractions for minimum $\Delta$. (This Table lists the polymers, 3, 2 and single component solvent mixtures with their solubility parameter components in the order $\delta_{d}, \delta_{p}, \delta_{h}$, the volume fractions $\phi$ corresponding to the minimum value of $\Delta$ and the $\Delta$ value. All solubility parameters in $\mathrm{J}^{1 / 2} / \mathrm{cm}^{3 / 2}$ )

| Case no. | Polymer |  |  | Solvents $b$ | $\delta_{d}$ | $\delta_{p}$ | ${ }^{\delta} h$ | Solvent volume fraction | $\Delta_{\left(J^{1 / 2} / \mathrm{cm}^{3 / 2}\right)}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Polybutadiene ${ }^{\text {a }}$ |  |  |  |  |  |  |  |  |
|  | 17.00 | 0 | 1.02 | Toluene | 18.05 | 1.4 | 2.0 | -0.123 |  |
|  |  |  |  | Hexane | 14.78 | 0 | 0 | 1.068 | 0.522 |
|  |  |  |  | Chlorobenzene | 19.00 | 4.3 | 2.0 | 0.055 |  |
| 2 |  |  |  | Toluene |  |  |  | 0.546 | 0.884 |
|  |  |  |  | Hexane |  |  |  | 0.454 |  |
| 3 |  |  |  | Toluene |  |  |  | 1.561 | 0.168 |
|  |  |  |  | Chlorobenzene |  |  |  | -0.561 |  |
| 4 |  |  |  | Toluene |  |  |  | 1.000 | 2.057 |
| 5 |  |  |  | Hexane |  |  |  | 1.000 | 2.399 |
| 6 | Polyacrylonitrile ${ }^{\text {a }}$ |  |  | Chlorobenzene |  |  |  | 1.000 | 4.851 |
| 7 |  |  |  |  |  |  |  |  |  |
|  | $18.24$ | $16.17$ | 6.75 | Ethyl acetate | 15.23 | 5.3 | 9.2 | 0.022 |  |
|  |  |  |  | Nitromethane | 15.76 | 18.8 | 5.1 | 0.819 | 2.845 |
|  |  |  |  | Chlorobenzene | 19.00 | 4.3 | 2.0 | 0.159 |  |
| 8 |  |  |  | n-Butyl acetate | 15.70 | 3.7 | 6.3 | 0.013 |  |
|  |  |  |  | Nitromethane |  |  |  | $0.823$ | 2.997 |
|  |  |  |  | Chlorobenzene |  |  |  | 0.164 |  |
| 9 |  |  |  | n-Propanol | 14.90 | 6.7 | 17.4 | 0.015 |  |
|  |  |  |  | Nitromethane |  |  |  | 0.801 | 2.397 |
|  |  |  |  | Chlorobenzene |  |  |  | 0.184 |  |
| 10 |  |  |  | n-Butyl lactate | 17.60 | 6.5 | 10.2 | 0.023 |  |
|  |  |  |  | Nitromethane |  |  |  | 0.816 | 2.505 |
|  |  |  |  | Chlorobenzene |  |  |  | 0.161 |  |
| 11 |  |  |  | Dimethylformamide | 17.44 | 13.7 | 11.2 | 1.218 |  |
|  |  |  |  | Nitromethane |  |  |  | $0.024$ | 1.848 |
|  |  |  |  | Chlorobenzene |  |  |  | -0.242 |  |
| 12 |  |  |  | Nitromethane |  |  |  | 0.819 | 2.849 |
|  |  |  |  | Chlorobenzene |  |  |  | 0.180 |  |
| 13 |  |  |  | Dimethyl formamide |  |  |  | 0.417 | 2.069 |
|  |  |  |  | Nitromethane |  |  |  | 0.583 |  |
| 14 |  |  |  | Dimethylformamide |  |  |  | 1.000 | 5.191 |
| 16 |  |  |  | Nitromethane |  |  |  | 1.000 | 5.518 |
|  | Nylon-66a |  |  |  |  |  |  |  |  |
|  | 18.54 | 5.12 | 12.28 | n-Propanol | 14.90 | 6.7 | 17.4 | 0.040 |  |
|  |  |  |  | Water ${ }^{\mathrm{c}}$ | 12.28 | 81.3 | 34.2 | 0.072 | 1.760 |
|  |  |  |  | Trichlorethylene | 17.97 | 3.1 | 5.3 | 0.888 |  |
| 17 |  |  |  | n-Propanol |  |  |  | 0.551 | 1.760 |
|  |  |  |  | Trichlorethylene |  |  |  | 0.449 |  |
| 18 | Poly(methyl methacrylate) ${ }^{\text {b }}$ |  |  |  |  |  |  |  |  |
|  | $15.74$ | $8.2$ | $6.7$ | Chloroform | 17.70 | 3.1 | 5.7 | 0.000 |  |
|  |  |  |  | Benzene | $18.32$ | 1.0 | 2.0 | 0.088 | 0.397 |
|  |  |  |  | MEK | 15.70 | 9.0 | 5.1 | 0.912 |  |
| 19 |  |  |  | MEK |  |  |  | 1.000 | 1.838 |
| 20 |  |  |  | Benzene |  |  |  | 1.000 | 8.953 |
| 21 |  |  |  | Chloroform |  |  |  | 1.000 | 5.668 |
| 22 | PVCa |  |  | Chloroform | 17.70 | 3.1 | 5.7 | 0.075 |  |
|  | 18.73 | 10.0 | 3.1 | Tetrahydrofuran | 16.82 | 5.7 | 8.0 | 3.400 | 0.426 |
|  |  |  |  | Butyl acetate | 15.70 | 3.9 | 6.3 | -2.475 |  |
| 23 |  |  |  | Chloroform | 17.70 | 3.1 | 5.7 | 0.567 | 3.038 |
|  |  |  |  | Nitromethane | 15.76 | 18.8 | 5.1 | 0.433 |  |
| 24 |  |  |  | Nitromethane | 15.76 | 18.8 | 5.1 | 0.476 | 1.846 |
|  |  |  |  | Toluene | 18.05 | 1.4 | 2.0 | 0.524 |  |
| 25 |  |  |  | Nitromethane | 15.76 | 18.8 | 5.1 | 0.099 | 3.480 |
|  |  |  |  | MEK | 15.90 | 9.0 | 5.1 | 0.990 |  |
| 26 |  |  |  | Tetrahydrofuran |  |  |  | 1.000 | 6.800 |
| 27 |  |  |  | Nitromethane |  |  |  | 1.000 | 9.510 |
| 28 |  |  |  | MEK |  |  |  | 1.000 | 5.635 |
| 29 |  | tereph | alate) |  |  |  |  |  |  |
|  | $19.52$ | $3.5$ | 8.6 | Chlorobenzene | 19.00 | 4.3 | 2.0 | 0.125 |  |
|  |  |  |  | Tolvene | 18.05 | 1.4 | 2.0 | 0.441 | 4.366 |
|  |  |  |  | Cyclohexanone | 17.70 | 8.4 | 5.1 | 0.434 |  |
| 30 |  |  |  | Chlorobenzene |  |  |  | 0.081 |  |
|  |  |  |  | Toluene |  |  |  | 0.681 | 3.232 |
|  |  |  |  | Dimethylformamide | 17.44 | 13.7 | 11.3 | 0.238 |  |
| 31 |  |  |  | Chlorobenzene |  |  |  | 0.035 |  |
|  |  |  |  | Toluene |  |  |  | 0.301 | 3.183 |
|  |  |  |  | Tetrahydrofuran |  |  |  | 0.664 |  |
| 32 |  |  |  | Chlorobenzene |  |  |  | 0.099 |  |
|  |  |  |  | Toluene |  |  |  | 0.703 | 3.314 |
|  |  |  |  | Dimethyl sulphoxide | 18.42 | 16.4 | 10.2 | 0.198 |  |

a Values from $K$ oenhen and Smolders ${ }^{3}$ converted to SI units; b values from Hansen ${ }^{2}$ converted to SI units; c note Hansen's ${ }^{2}$ statement:
'The placement of water at $7.0,8.0$ and $20.9\left(\mathrm{cal}^{1 / 2} / \mathrm{cm}^{3 / 2}\right)$ is perhaps more symbolic than reliable'. He later uses the figures given, presumably after recalculation

## Letters

It must be noted that nothing is mentioned about the proportions of the components of the liquids absorbed by crosslinked or insoluble polymers which may be very different from that in the ambient mixture. Some reservations must also be made concerning the use of relative weight increases in view of the different densities of the pure materials involved; it is necessary, for a common basis, to express all
results as relative volume increase.

## CONCLUSIONS

A method for the calculation of most efficient mixtures of three, two or single component solvents for resins has been developed. This method, because of its rapidity using modern computers, is capable of screening many
combinations. The best of these may then be tested experimentally.

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## Letters

## The microstructure of polychloroprene determined by ${ }^{13} \mathrm{C}$-nuclear magnetic resonance

The properties of polydienes are dependent upon the configurations of the diene units within the chains, the distribution of these units along the chain and upon the relative orientations of the units, i.e. whether they are in head-head, head-tail or tailtail arrangements. ${ }^{13} \mathrm{C}$ nuclear magnetic resonance ( ${ }^{13} \mathrm{C}$ n.m.r.) spectroscopy can be used not only to distinguish between polybutadienes and polyisoprenes with regular microstructures ${ }^{1}$ but also to determine the relative amounts and the distributions of diene units with different configurations within polymers of irregular microstructure ${ }^{2-12}$. It has been shown also that for polyisoprenes, ${ }^{13} \mathrm{C}$ n.m.r. can be used to identify and measure the relative amounts of head-head, head-tail and tail-tail linkages involving 1,4- units ${ }^{11,12}$.

For polychloroprenes, proton magnetic resonance spectroscopy can be used to detect head-head and tail-tail linkages between 1,4 - units ${ }^{13}$ and also, if high field strengths are employed, to determine the relative amounts of cis-1,4- and trans-1,4- enchainment ${ }^{14}$. As yet, there have been no publications describing the use of ${ }^{13} \mathrm{C}$ n.m.r. to determine the microstructure of polychloroprenes, although the technique has been used to give some limited information regarding the microstructure of some chloroprene-methyl methacrylate copolymers ${ }^{15}$.

The Figure shows the methylene carbon resonances obtained at 20 MHz
(Varian CFT20 spectrometer) for a sample of polychloroprene prepared by bulk thermal polymerization under nitrogen at $25^{\circ} \mathrm{C}$. The spectrum is the result of 30 K pulses on a $10 \% \mathrm{w} / \mathrm{v}$ solution of the polymer in $\mathrm{CDCl}_{3}$ with an acquisition time of 0.5 sec and a pulse width of $12 \mu \mathrm{sec}$ (corresponding to a nuclear tip angle of $\sim 51^{\circ}$ ). There was no additional delay between pulses. 4096 data points were used in the accumulation of the spectrum over a spectral width of 4000 Hz , and the usual 'white noise' proton decoupling procedure was employed. The relative areas of the peaks in the spectrum were not affected by small changes in


Figure 1 Methylene carbon resonances in polychloroprene (Peak assignments are given in the text)


[^0]:    * An APL program which has been written by the author's associates, Mr B. Grinbaum and Mr G. Friedman, prints out the results as:
    $\begin{array}{lll}a_{1} & a_{2} & a_{3}\end{array}$
    $b_{1} b_{2} b_{3}$
    $c_{1} c_{2} c_{3}$
    $p_{1} p_{2} p_{3} \Delta m_{1} m_{2} m_{3} \phi_{a} \phi_{b} \phi_{C}$

